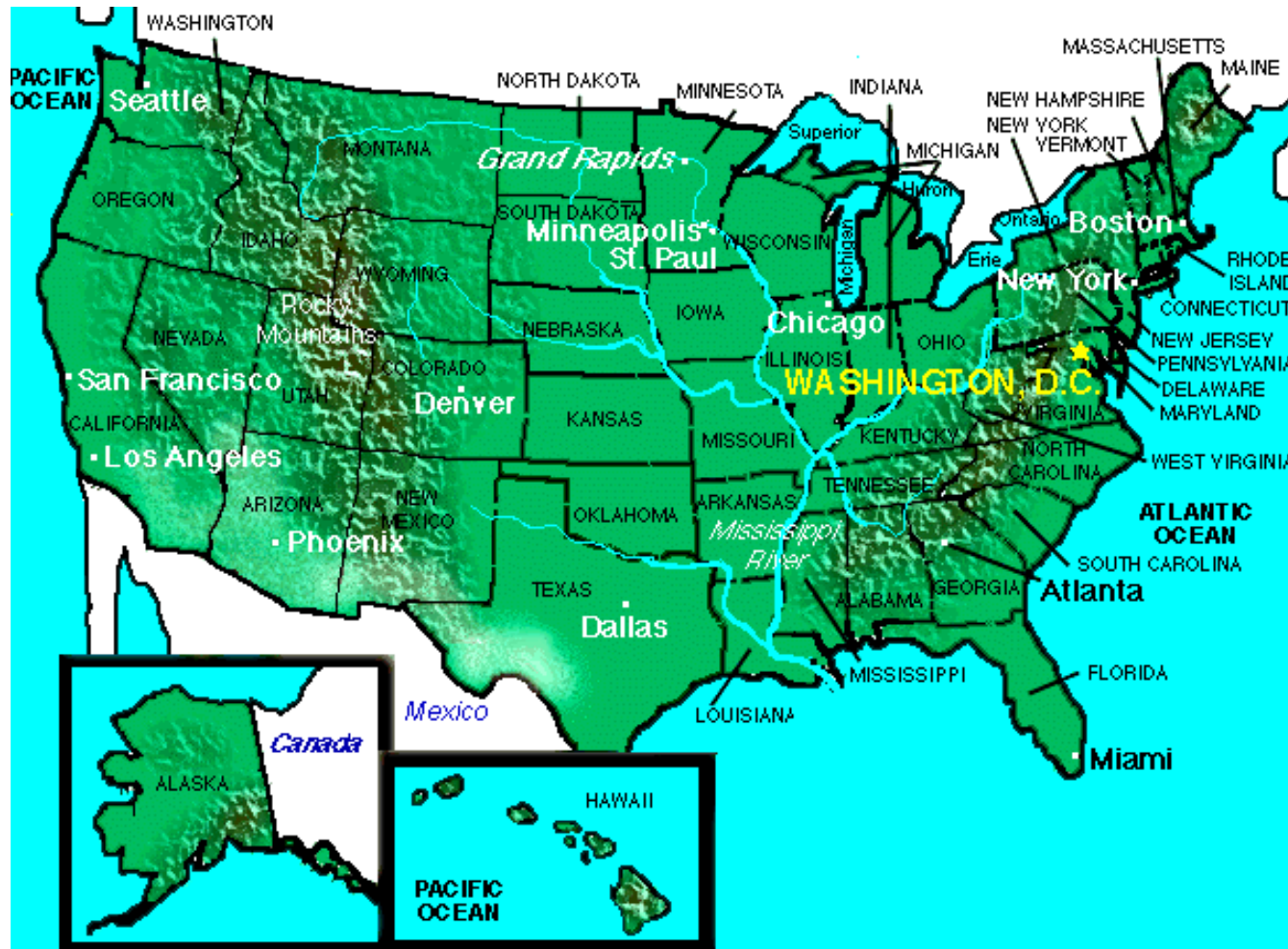


Example: Map coloring



Dynamic backtracking

- $expl_{ik}$
 - explanation for *eliminating* the value v_k for variable x_i
 - set of previously assigned variables that imply that x_i cannot take the value v_k
 - analogous to a combination of mcl_{ik} and $conf-set_i$ generalized to non-binary constraints
 - can be set by forward or backward checking
- *assigned*
 - sequence of assigned variables
- *unassigned*
 - set of unassigned variables

Dynamic backtrack: *label*

```
function dbt-label(i)  
  update-explanations(i)  
  if  $CD_i \neq \{\}$  then  
    Select some  $v_k \in CD_i$  and set  $x_i = v_k$   
    push(i, assigned) and  $unassigned = unassigned \setminus \{i\}$   
    return (NextVar(), true)  
  else  
    return (i, false)  
end dbt-label
```

Updating eliminating explanations

```
procedure update-explanations(i)  
  for each  $v_k \in CD_i$  do  
    for each completed constraint  $C$  that refers to  $x_i$  do  
      if  $C$  is not satisfied then  
         $expl_{ik} = vars(C) \setminus \{x_i\}$   
         $CD_i = CD_i \setminus \{v_k\}$   
        break inner loop  
      endif  
    endfor  
  end update-explanations
```

Dynamic backtracking: *unlabel*

function *dbt-unlabel*(*i*)

$expl = \bigcup_r expl_{ir}$

if $expl = \{\}$ **then return** (0, *false*)

Let $j \in expl$ be the *last* element pushed onto *assigned* and

let v_k be currently assigned to x_j

for each l assigned *after* j and each value $v_m \in D_l$ **do**

if $j \in expl_{lm}$ **then**

$expl_{lm} = \{\}$

$CD_l = CD_l \cup \{v_m\}$

endif

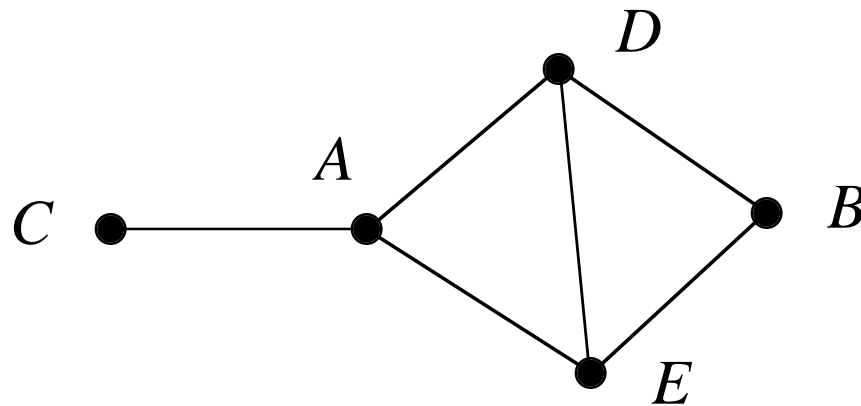
$assigned = assigned \setminus \{j\}$ and $unassigned = unassigned \cup \{j\}$

$expl_{jk} = expl \setminus \{j\}$

return (*NextVar*(), *true*)

end *dbt-unlabel*

Example



<i>Country</i>	<i>color</i>	<i>red</i>	<i>yellow</i>	<i>blue</i>
<i>A</i>				
<i>B</i>				
<i>C</i>				
<i>D</i>				
<i>E</i>				

Termination of dynamic backtracking

- Setting $expl_{ik} = \{y_1, \dots, y_l\}$ is equivalent to asserting the nogood

$$y_1 = d_1, \dots, y_l = d_l \Rightarrow x_i \neq v_k$$

- Let $\{s_1, \dots, s_m\}$ be the variables that *precede* x_i when $expl_{ik}$ is set
 \Rightarrow the following *modified nogood* is entailed

$$s_1 = e_1, \dots, s_m = e_m \Rightarrow x_i \neq v_k$$

- **Lemma:** As long as the modified nogood is entailed by some nogood, the algorithm will not visit the node

$$s_1 = e_1, \dots, s_m = e_m, x_i = v_k$$

- **Corollary:** Whenever a nogood is asserted, a previously unentailed modified nogood is entailed

Termination (contd.)

- **Lemma:** When the algorithm deletes a nogood, the corresponding modified nogood continues to be entailed
- **Corollary:** The set of entailed modified nogoods grows monotonically
- **Theorem:** Dynamic backtracking terminates